Data Structures and Algorithms for Engineers

Module 5: Lists

Lecture 2: List ADT: implementation with linked lists. Doubly linked lists and circular lists. Performance considerations.

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Aside:

Linked Lists Using Pointers

Why Pointer-Based Implementation?

- Linked lists are used avoid excessive data movement with insertions and deletions
- Elements are not necessarily stored in contiguous memory locations
- Makes efficient use of memory space
 - Allocate space when needed
 - Deallocate space when finished & return it to the free store
- Failure to deallocate space will cause memory leakage

Why Pointer-Based Implementation?

Some guidelines when writing programs that dynamically allocate memory

- Use malloc or new to create data-structures of the appropriate size
- Remember to avoid memory leakage by always using free and delete to deallocate dynamically-created data-structures
- Check every call to malloc or new to see if it returned NULL (i.e. check if the allocation was unsuccessful)

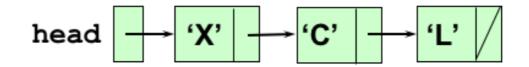
Why Pointer-Based Implementation?

Some guidelines when writing programs that dynamically allocate memory

- You must expect free or delete to alter the contents of the memory that was freed or deleted
- Never access a data structure after it has been freed or deleted
- If malloc fails in a non-interactive program, make that a fatal error
- In an interactive program, it is better to abort the current command and return to the command reader loop

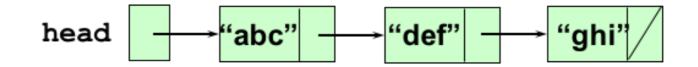
A Linked List

- A linked list is a list in which the order of the components is determined by an explicit link member in each node
- The nodes are structs
 - each node contains a component member and also a link member that gives the location of the next node in the list



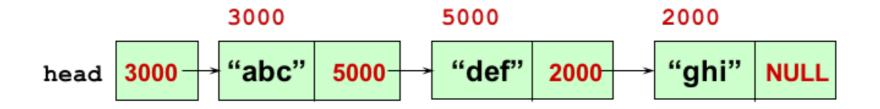
Pointer-Based (Dynamic) Linked List

A pointer-based linked list is a dynamic linked list where nodes are linked together by pointers, and an external pointer (or head pointer) points to the first node in the list

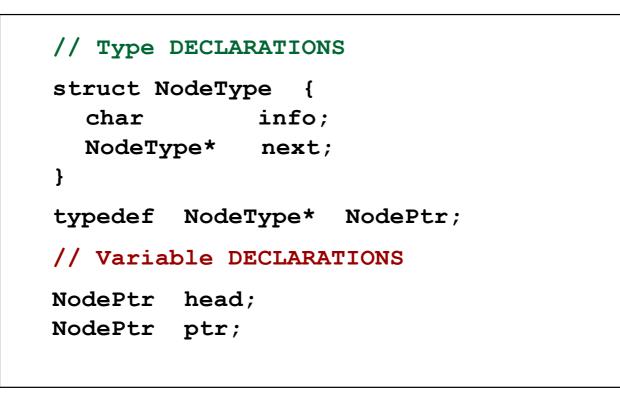


Nodes can be located anywhere in memory

The link member holds the memory address of [or a reference to, i.e., pointer to] the next node in the list

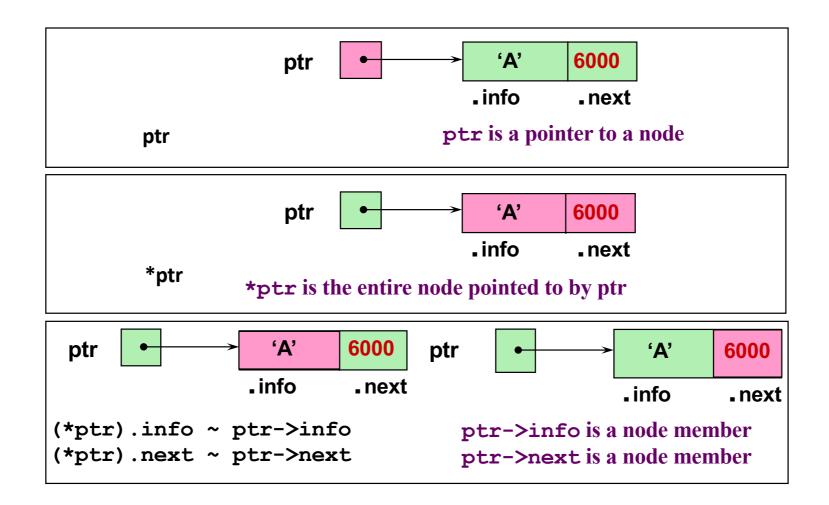


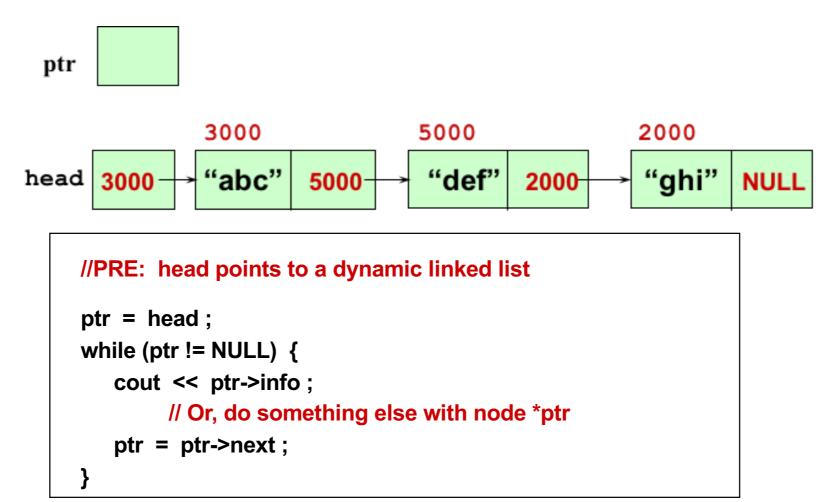
Declarations for a Dynamic Linked List

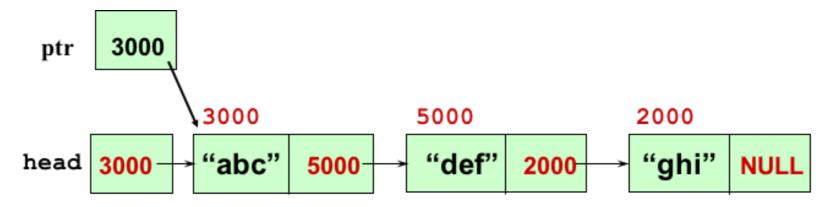




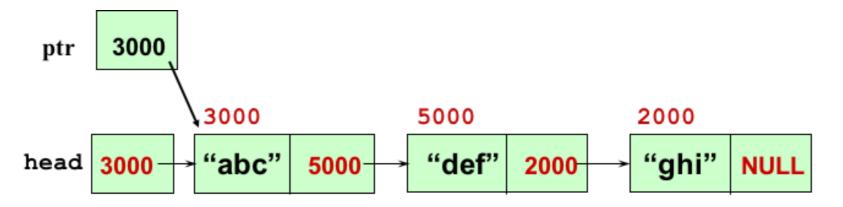
Pointer Dereferencing and Member Selection

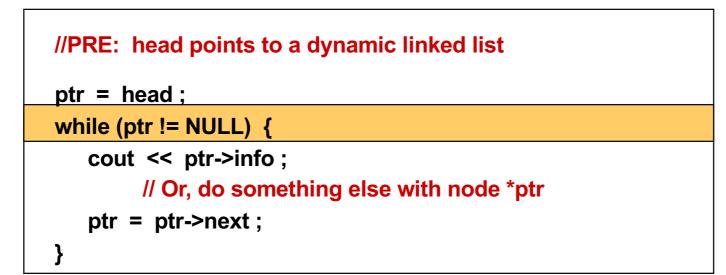


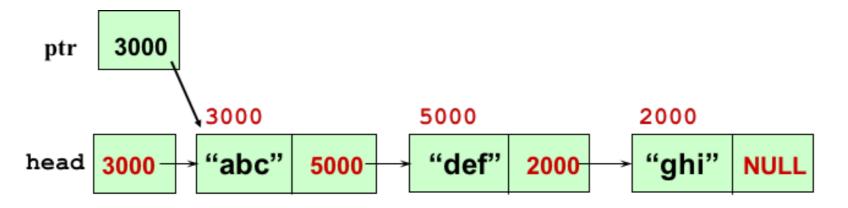


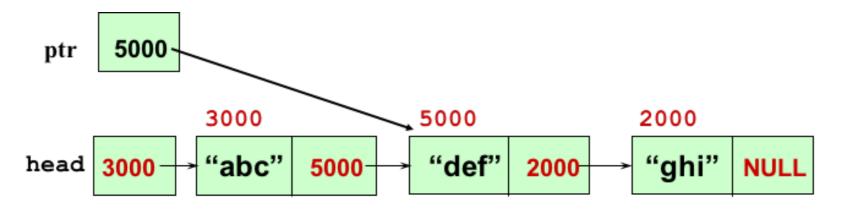


//PRE: head points to a dynamic linked list
ptr = head;
while (ptr != NULL) {
 cout << ptr->info;
 // Or, do something else with node *ptr
 ptr = ptr->next;
}

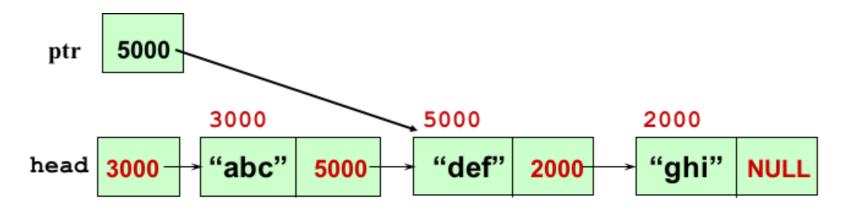


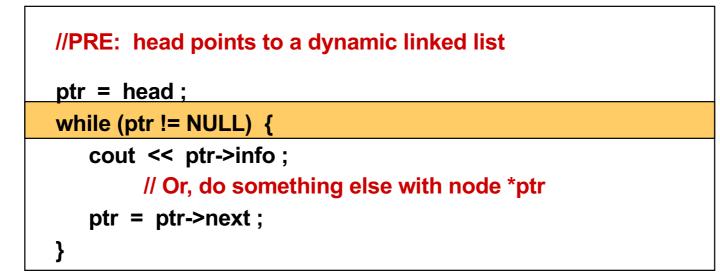


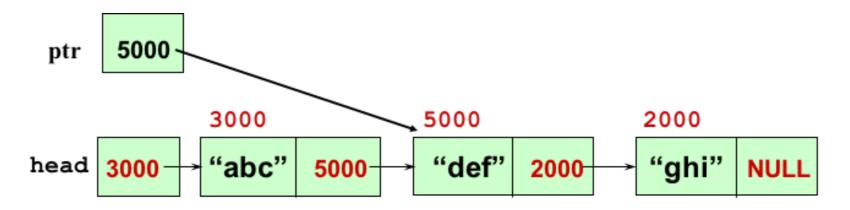




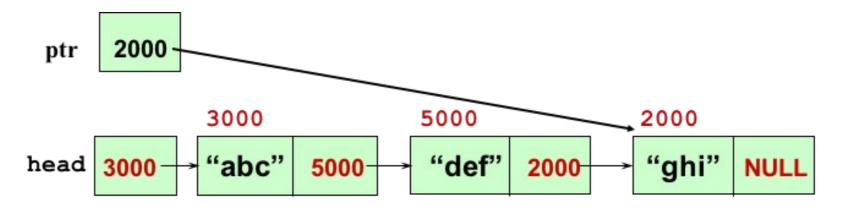
```
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ptr = head;
while (ptr != NULL) {
    cout << ptr->info;
        // Or, do something else with node *ptr
    ptr = ptr->next;
}
```



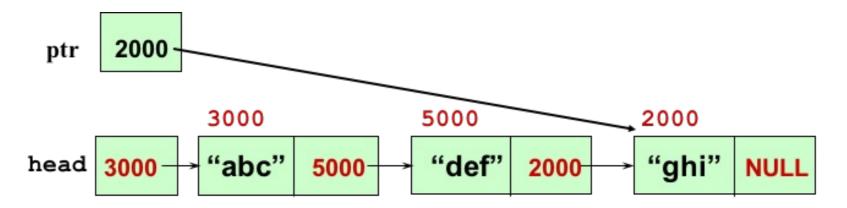


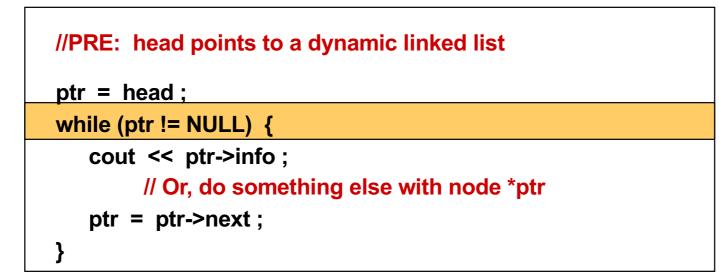


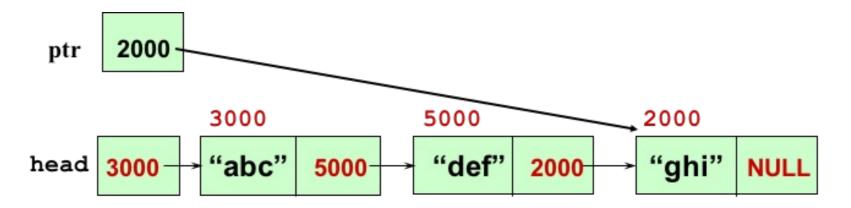
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}
```



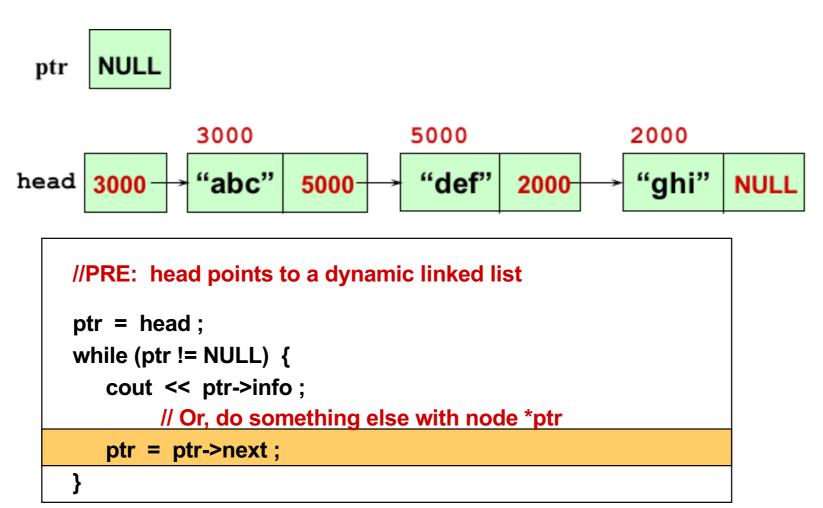
```
//PRE: head points to a dynamic linked list
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    ptr = ptr->next;
}
```

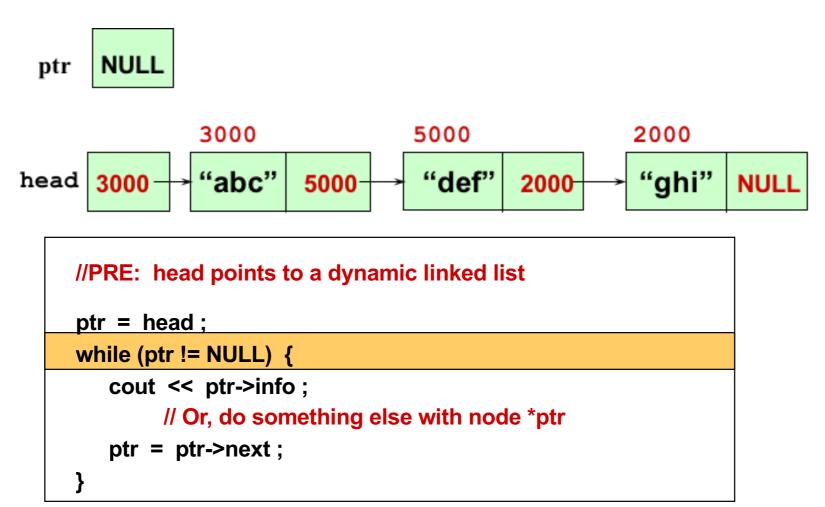






```
//PRE: head points to a dynamic linked list
ptr = head;
while (ptr != NULL) {
    cout << ptr->info;
    // Or, do something else with node *ptr
    ptr = ptr->next;
}
```





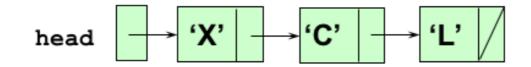
Using Operator <u>new</u>

- If memory is available in an area called the free store (or heap), operator <u>new</u> allocates the requested object, and returns a pointer to the memory allocated
- The dynamically allocated object exists until the delete operator destroys it

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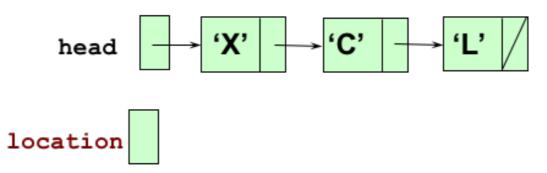


char	<pre>item = `B';</pre>	
NodePtr	location;	
location	= new NodeType;	
location	<pre>location->info = item;</pre>	
<pre>location->next = head;</pre>		
head = 1c	ocation;	



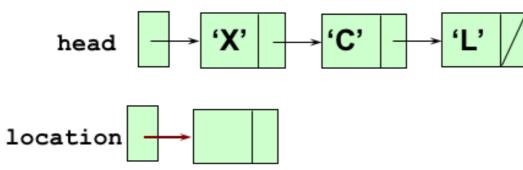


char	item = `B';
NodePtr	location;
location	= new NodeType;
<pre>location->info = item;</pre>	
<pre>location->next = head;</pre>	
head = 1	ocation;



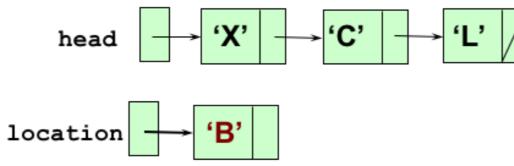


char	item = 'B';
NodePtr	location;
location	= new NodeType;
<pre>location->info = item;</pre>	
<pre>location->next= head;</pre>	
head = 1	ocation;



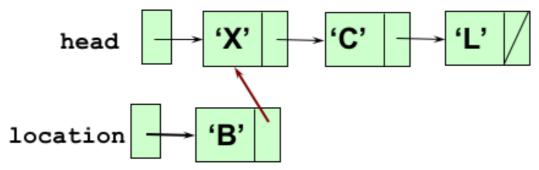


char	<pre>item = `B';</pre>
NodePtr	location;
location	= new NodeType;
<pre>location->info = item;</pre>	
<pre>location->next= head;</pre>	
head = 1	ocation;

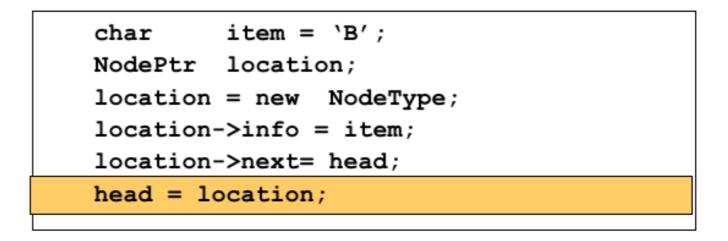


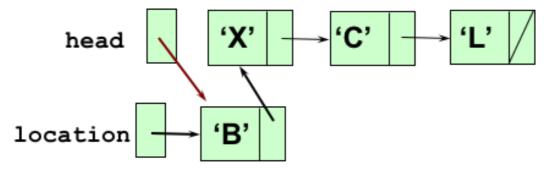


char	<pre>item = `B';</pre>
NodePtr	location;
location	= new NodeType;
<pre>location->info = item;</pre>	
<pre>location->next= head;</pre>	
<pre>head = location;</pre>	









Using Operator delete

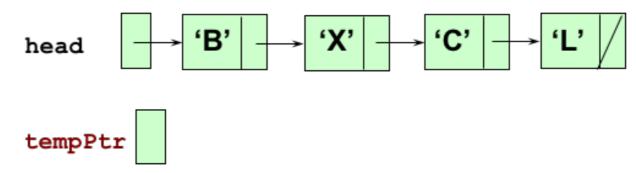
The object currently pointed to by the pointer is deallocated, and the pointer is considered undefined.

The object's memory is returned to the free store.

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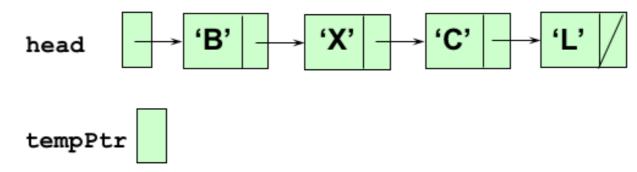


NodePtr tempPtr;	
<pre>item = head->info;</pre>	
tempPtr = head;	
head = head-> next	
delete tempPtr;	



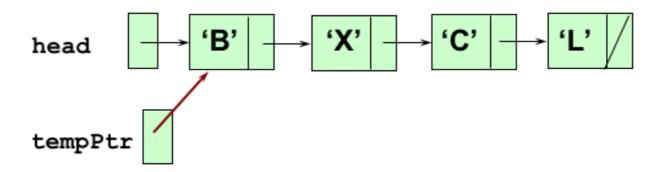


NodeType * tempPtr;	
<pre>item = head->info;</pre>	
<pre>tempPtr = head;</pre>	
head = head-> next	
delete tempPtr;	



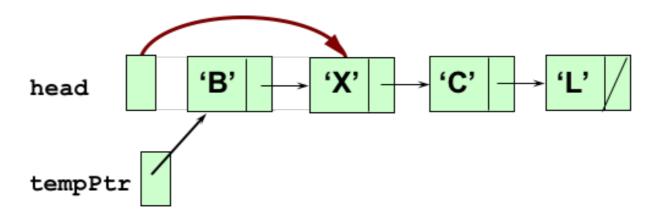


NodeType * tempPtr;	
<pre>item = head->info;</pre>	
<pre>tempPtr = head;</pre>	
head = head-> next	
delete tempPtr;	



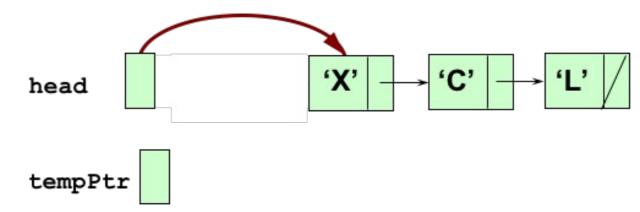


NodeType * tempPtr;
<pre>item = head->info;</pre>
<pre>tempPtr = head;</pre>
head = head-> ^{next}
delete tempPtr;



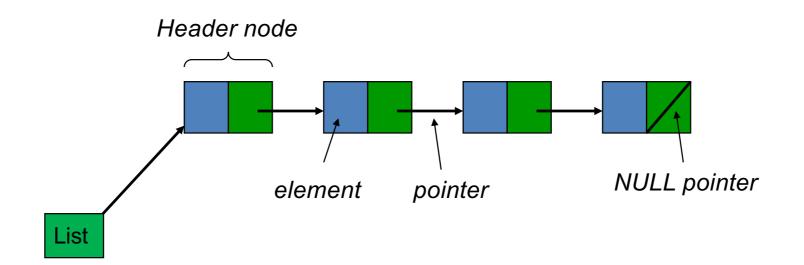


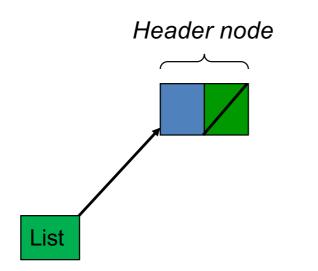
NodeType * tempPtr;
<pre>item = head->info;</pre>
<pre>tempPtr = head;</pre>
head = head-> ^{next}
delete tempPtr;



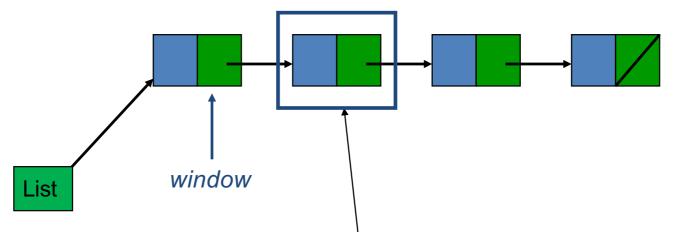
End of Aside:

Linked Lists Using Pointers

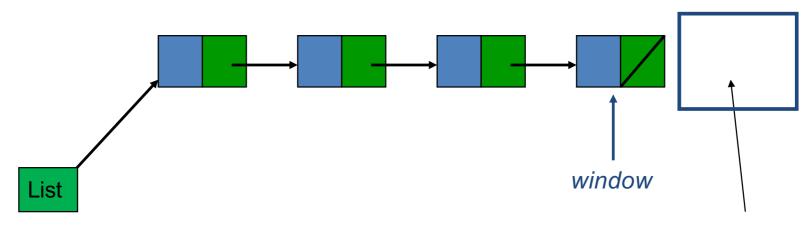




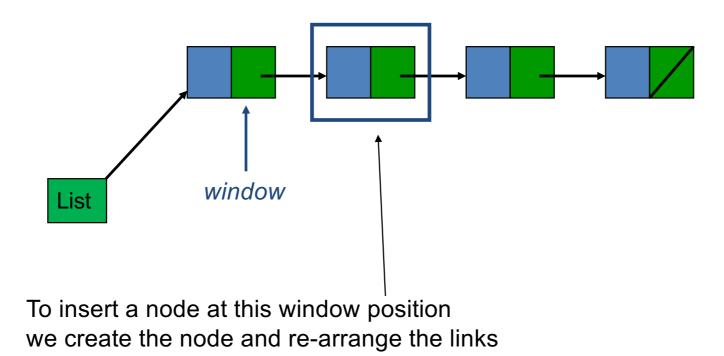
An empty list!!!

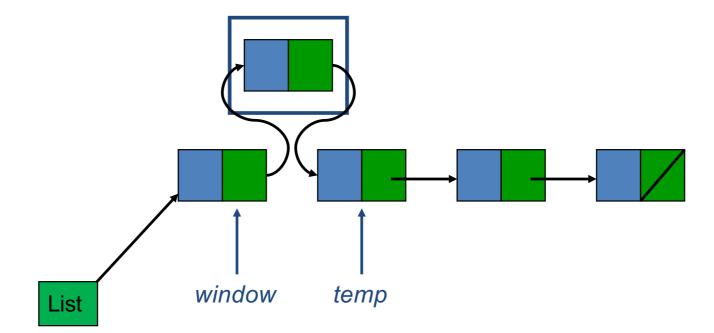


To place the window at this position we provide a link to the previous node (hence the need for a header node) When we insert and delete nodes, we have to modify the link in the previous node. If we didn't have a pointer to the previous node, we would have to run the list from the start to find it. This would mean that insert and delete operations would be O(n), instead of O(1)

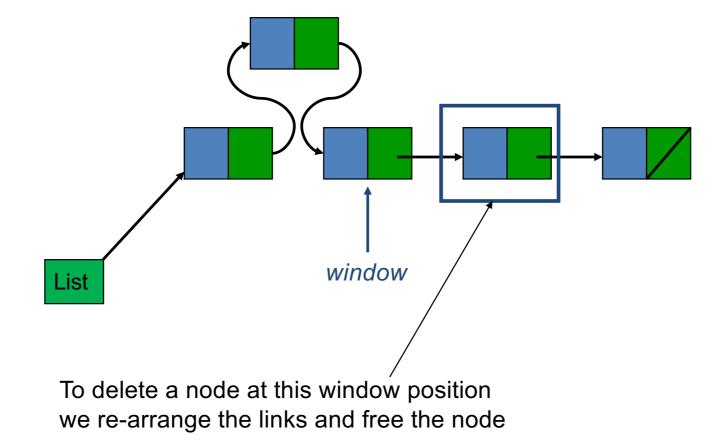


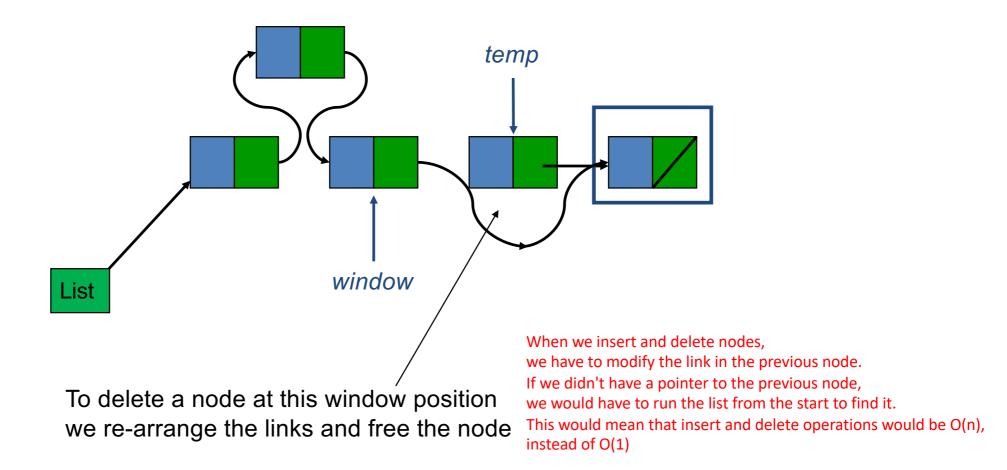
To place the window at end of the list we provide a link to the last node

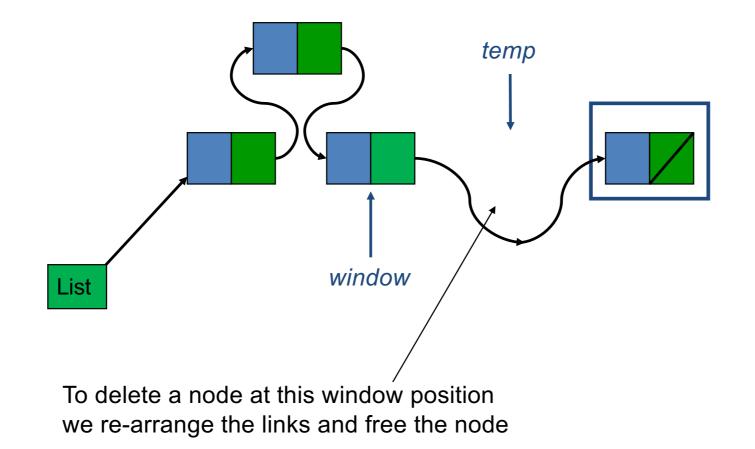




To insert a node at this window position we create the node and re-arrange the links When we insert and delete nodes, we have to modify the link in the previous node. If we didn't have a pointer to the previous node, we would have to run the list from the start to find it. This would mean that insert and delete operations would be O(n), instead of O(1)







- type elementtype
- type LIST
- type Boolean
- type windowtype

/* linked-list implementation of LIST ADT */

#include <stdio.h>
#include <math.h>
#include <string.h>

#define FALSE 0
#define TRUE 1

```
typedef struct {
    int number;
    char *string;
} ELEMENT_TYPE;
```



typedef struct node *NODE_TYPE;

typedef struct node {

} NODE;

ELEMENT_TYPE element; NODE TYPE next;

number
string

typedef NODE_TYPE LIST_TYPE;
typedef NODE TYPE WINDOW TYPE;

```
typedef struct node *NODE_TYPE;
/* alternative approach ... */
/* but need to use sizeof(struct node) in malloc()*/
struct node {
    ELEMENT_TYPE element;
    NODE_TYPE next;
    };
```

typedef NODE_TYPE LIST_TYPE;
typedef NODE TYPE WINDOW TYPE;

```
/*** position following last element in a list ***/
```

```
WINDOW TYPE end(LIST TYPE *list) {
   WINDOW TYPE q;
   q = *list;
   if (q == NULL) {
      error("non-existent list");
   }
   else {
      while (q->next != NULL) {
          q = q - next;
       }
                               number
                                               number
                                                               number
                               string
                                               string
                                                               string
   return(q);
                    *list
}
                                   q
```

```
/*** position following last element in a list ***/
```

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          q = q - next;
       }
                                               number
                                                               number
                               number
                               string
                                               string
                                                               string
   return(q);
                    *list
}
                                                   q
```

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   }
   else {
      while (q->next != NULL) {
          q = q - next;
       }
                                               number
                                                               number
                               number
                               string
                                               string
                                                               string
   return(q);
                    *list
}
                                                                  a
```

```
/*** empty a list ***/
WINDOW TYPE empty(LIST TYPE *list) {
   WINDOW TYPE p, q;
   if (*list != NULL) {
      /* list exists: delete all nodes including header */
      q = *list;
      while (q->next != NULL) {
         p = q;
         q = q - next;
         free(p);
       }
                              number
                                             number
                                                            number
      free(q)
                              string
                                             string
                                                            string
                   *list
                                 q
```

```
/*** empty a list ***/
WINDOW TYPE empty(LIST TYPE *list) {
   WINDOW TYPE p, q;
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      q = *list;
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         p = q;
         q = q - next;
         free(p);
       }
                              number
                                             number
                                                            number
      free(q)
                              string
                                             string
                                                             string
                   *list
                                 q
                              р
```

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         q = q - next;
          free(p);
       }
                                             number
                                                            number
                              number
      free(q)
                              string
                                             string
                                                            string
                   *list
```

р

```
/*** empty a list ***/
```

```
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      q = *list;
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         q = q - next;
         free(p);
      }
                                                           number
                                            number
      free(q)
                                            string
                                                           string
                   *list
```

р

```
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         p = q;
         q = q - next;
         free(p);
      }
                                                           number
                                            number
      free(q)
                                            string
                                                           string
                   *list
```

р

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         p = q;
         q = q - next;
         free(p);
      }
                                                           number
                                            number
      free(q)
                                            string
                                                           string
                   *list
```

q

р

```
/*** empty a list ***/
```

```
WINDOW TYPE empty(LIST TYPE *list) {
   WINDOW TYPE p, q;
   if (*list != NULL) {
      /* list exists: delete all nodes including header */
      q = *list;
      while (q->next != NULL) {
         p = q;
         q = q - next;
         free(p);
      }
                                                          number
      free(q)
                                                          string
                   *list
                                                             q
                                            р
```

```
/*** empty a list ***/
WINDOW_TYPE empty(LIST_TYPE *list) {
    WINDOW_TYPE p, q;
    if (*list != NULL) {
```

```
/* list exists: delete all nodes including header */
q = *list;
```

```
while (q->next != NULL) {
```

```
p = q;
```

```
q = q - next;
```

```
free(p);
```

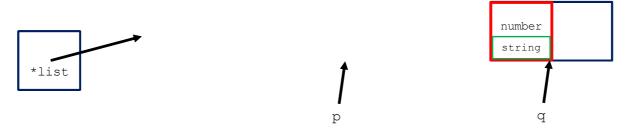
```
}
free(q);
*list
```

q

р

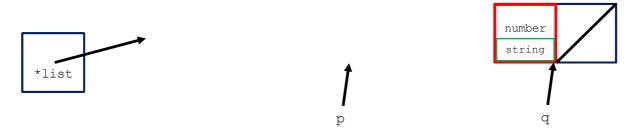
```
/* now, create a new empty one with a header node */
```

```
if ((q = (NODE_TYPE) malloc(sizeof(NODE))) == NULL)
    error("function empty: unable to allocate memory");
else {
    q->next = NULL;
    *list = q;
}
return(end(list));
```



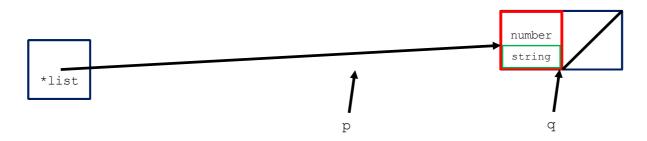
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    *list = q;
}
return(end(list));
```



```
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```

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if ((q = (NODE_TYPE) malloc(sizeof(NODE))) == NULL)
    error("function empty: unable to allocate memory");
else {
    q->next = NULL;
    *list = q;
}
return(end(list));
```



```
/*** test to see if a list is empty ***/
int is_empty(LIST_TYPE *list) {
   WINDOW TYPE q;
   q = *list;
   if (q == NULL) {
      error("non-existent list");
   }
   else {
                                                              number
      if (q->next == NULL) {
                                                               string
          return (TRUE);
                                                   *list
      else
          return(FALSE);
                               number
                                               number
                                                               number
                               string
                                               string
                                                               string
}
                    *list
```

```
/*** position at first element in a list ***/
WINDOW TYPE first(LIST TYPE *list) {
   if (is_empty(list) == FALSE) {
      return(*list);
   else
      return(end(list));
                                                             number
}
                                                             string
                                                  *list
                                                           end(list)
                              number
                                              number
                                                             number
```

string

*list

string

string

```
/*** position at next element in a list ***/
WINDOW TYPE next (WINDOW TYPE w, LIST TYPE *list) {
   if (w == last(list)) {
      return(end(list));
   else if (w == end(list)) {
      error("can't find next after end of list");
   else {
      return (w->next);
                                                             number
                              number
                                             number
                              string
                                             string
                                                             string
                    *list
                                                          end(list)
                                            w->next
```

```
/*** position at previous element in a list ***/
```

```
WINDOW TYPE previous (WINDOW TYPE w, LIST TYPE *list) {
  WINDOW TYPE p, q;
   if (w != first(list)) {
     p = first(list);
     while (p->next != w) {
         p = p - > next;
         if (p == NULL) break; /* trap this to ensure */
                               /* we don't dereference */
      }
      if (p != NULL) /* a null pointer in the */
         return(p); /* while condition
                                                         */
            number
                          number
                                        number
                                                      number
            string
                          string
                                        string
                                                      string
   *list
```

```
/*** position at previous element in a list ***/
```

string

*list

```
WINDOW TYPE previous (WINDOW TYPE w, LIST TYPE *list) {
  WINDOW TYPE p, q;
  if (w != first(list)) {
     p = first(list);
     while (p->next != w) {
        p = p - > next;
        if (p == NULL) break; /* trap this to ensure */
                              /* we don't dereference */
      }
     if (p != NULL) /* a null pointer in the */
        return(p); /* while condition
                                                       */
            number
                         number
                                      number
                                                   number
```

string

string

string

```
else {
    error("can't find previous to a non-existent node");
    }
else {
    error("can't find previous before first element of list");
    return(w);
}
```

```
/*** position at last element in a list ***/
WINDOW_TYPE last(LIST_TYPE *list) {
   WINDOW_TYPE p, q;
   if (*list == NULL) {
      error("non-existent list");
   }
   else {
      /* list exists: find last node */
```

```
/* list exists: find last node */
   if (is_empty(list)) {
      p = end(list);
   }
   else {
      p = *list;
      q = p - next;
      while (q->next != NULL) {
          p = q;
          q = q - next;
                              number
                                              number
                                                              number
   }
                                              string
                              string
                                                              string
   return(p);
                   *list
}
                               р
                                              q
```

```
/* list exists: find last node */
   if (is_empty(list)) {
       p = end(list);
   }
   else {
       p = *list;
       q = p - next;
       while (q->next != NULL) {
           p = q;
           q = q - \operatorname{next};
                                number
                                                 number
                                                                  number
    }
                                string
                                                 string
                                                                  string
   return(p);
                    *list
}
                                               р
                                                 q
```

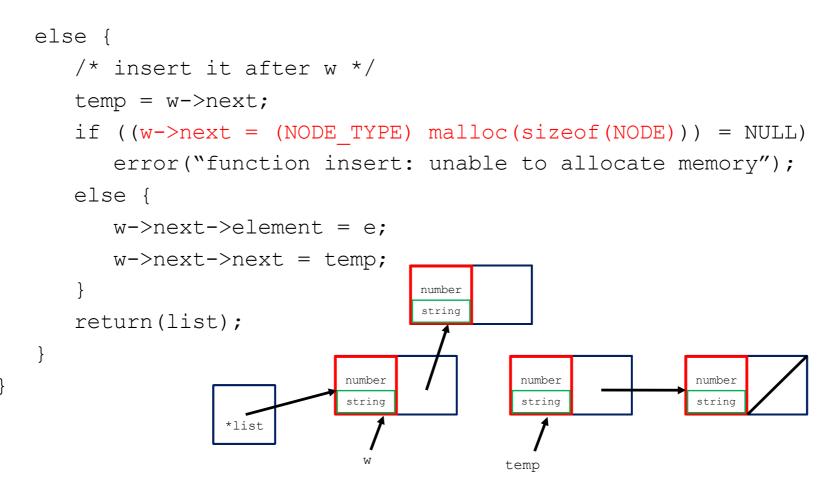
```
/* list exists: find last node */
   if (is_empty(list)) {
       p = end(list);
    }
   else {
       p = *list;
       q = p - next;
       while (q->next != NULL) {
           p = q;
           q = q - \operatorname{next};
                                number
                                                  number
                                                                   number
    }
                                string
                                                  string
                                                                   string
   return (p) ;
                    *list
}
                                                р
                                                                   q
```

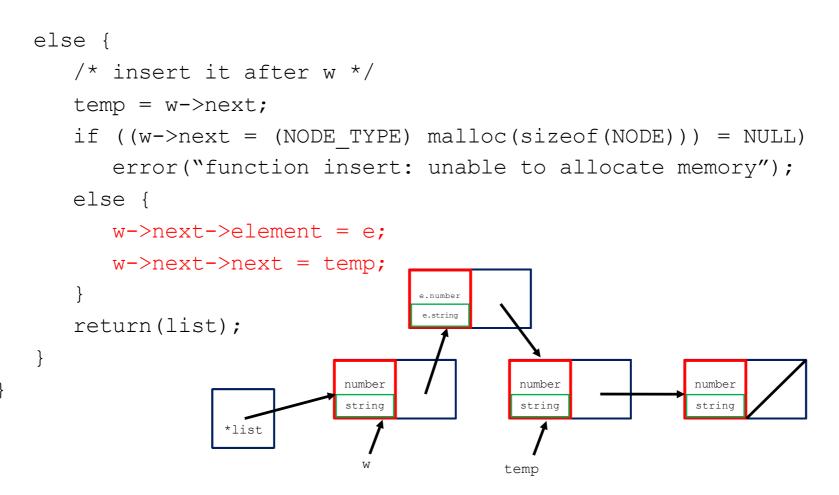
```
/*** insert an element in a list ***/
```

```
LIST_TYPE *insert(ELEMENT_TYPE e, WINDOW_TYPE w,
                    LIST_TYPE *list) {
    WINDOW_TYPE temp;
    if (*list == NULL) {
        error("cannot insert in a non-existent list");
    }
```

```
else {
   /* insert it after w */
   temp = w->next;
   if ((w->next = (NODE_TYPE) malloc(sizeof(NODE))) = NULL)
      error ("function insert: unable to allocate memory");
   else {
      w->next->element = e;
      w->next->next = temp;
   }
   return(list);
                                                         number
                           number
                                          number
                           string
                                          string
                                                         string
                *list
                                         temp
```

}





```
/*** delete an element from a list ***/
LIST TYPE *delete(WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p;
   if (*list == NULL) {
      error("cannot delete from a non-existent list");
   else {
      p = w->next; /* node to be deleted */
      w->next = w->next->next; /* rearrange the links */
      free(p); /* delete the node */
      return(list);
                                           number
                                                         number
                            number
                            strina
                                           string
                                                         string
}
                  *list
                                           р
```

```
/*** delete an element from a list ***/
LIST TYPE *delete(WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p;
   if (*list == NULL) {
      error("cannot delete from a non-existent list");
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      p = w->next; /* node to be deleted */
      w->next = w->next->next; /* rearrange the links */
      free(p); /* delete the node */
      return(list);
                                                         number
                            number
                                          number
                            strina
                                          string
                                                         string
}
                  *list
```

```
/*** delete an element from a list ***/
LIST TYPE *delete(WINDOW TYPE w, LIST TYPE *list) {
   WINDOW TYPE p;
   if (*list == NULL) {
      error("cannot delete from a non-existent list");
   else {
      p = w->next; /* node to be deleted */
      w->next = w->next->next; /* rearrange the links */
      free(p); /* delete the node */
      return(list);
                                                        number
                            number
                                                        string
                            string
}
                  *list
```

```
/*** retrieve an element from a list ***/
```

```
ELEMENT_TYPE retrieve(WINDOW_TYPE w, LIST_TYPE *list) {
   WINDOW TYPE p;
```

```
if (*list == NULL) {
    error("cannot retrieve from a non-existent list");
}
else {
    return(w->next->element);
}
```

}

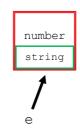
```
/*** print all elements in a list ***/
int print(LIST_TYPE *list) {
   WINDOW_TYPE w;
   ELEMENT_TYPE e;
```

```
printf("Contents of list: \n");
w = first(list);
while (w != end(list)) {
    e = retrieve(w, list);
    printf("%d %s\n", e.number, e.string);
    w = next(w, list);
}
printf("---\n");
return(0);
```

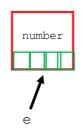
}

```
int error(char *s) {
    printf("Error: %s\n", s);
    exit(0);
}
```

```
/*** assign values to an element ***/
int assign_element_values(ELEMENT_TYPE *e, int number, char s[]) {
    e->string = (char *) malloc(sizeof(char) * (strlen(s)+1));
    strcpy(e->string, s);
    e->number = number;
}
```



```
/*** assign values to an element ***/
int assign_element_values(ELEMENT_TYPE *e, int number, char s[]) {
    e->string = (char *) malloc(sizeof(char) * (strlen(s)+1));
    strcpy(e->string, s);
    e->number = number;
}
```



```
void initialize_list(LIST_TYPE *list) {
    *list = NULL;
}
```

```
*iist
```

```
/*** main driver routine ***/
```

```
WINDOW_TYPE w;
ELEMENT_TYPE e;
LIST_TYPE list;
int i;
```

```
initialize_list(&list);
empty(&list);
print(&list);
```

```
assign_element_values(&e, 1, "String A");
w = first(&list);
insert(e, w, &list);
print(&list);
```

```
assign_element_values(&e, 2, "String B");
insert(e, w, &list);
print(&list);
```

```
assign_element_values(&e, 3, "String C");
insert(e, last(&list), &list);
print(&list);
```

```
assign_element_values(&e, 4, "String D");
w = next(last(&list), &list);
insert(e, w, &list);
print(&list);
```

```
w = previous(w, &list);
delete(w, &list);
print(&list);
```

}

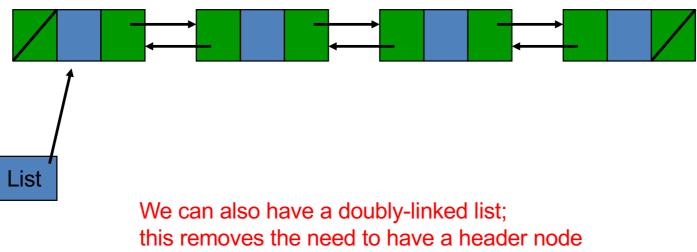
Key points:

- All we changed was the implementation of the data-structure and the access routines
- But by keeping the interface to the access routines the same as before, these changes are transparent to the user
- And we didn't have to make any changes in the main function which was actually manipulating the list

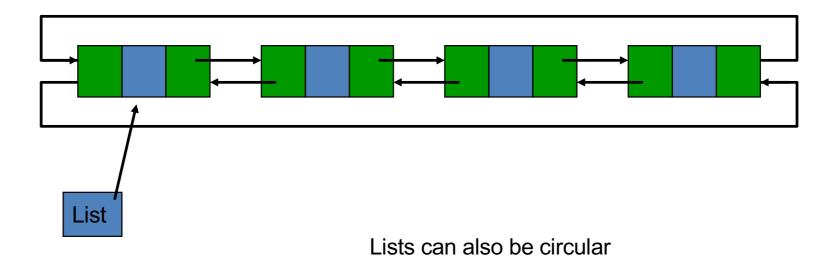
Key points:

- In a real software system where perhaps hundreds (or thousands) of people are using these list primitives, this transparency is critical
- We couldn't have achieved it if we manipulated the data-structure directly

- Possible problems with the implementation:
 - we have to run the length of the list in order to find the end
 (i.e., end(L) is O[n])
 - there is a (small) overhead in using the pointers
- On the other hand, the list can now grow as large as necessary, without having to predefine the maximum size



and make finding the previous node more efficient



Comparison: Linked Lists vs. Arrays

- Relative advantages of linked lists
 - Overflow on linked structures can never occur unless memory is actually full
 - Insertions and deletions are simpler than for contiguous (array) lists
 - With large records, moving pointers is easier and faster than moving the items themselves

Comparison: Linked Lists vs. Arrays

- Relative advantages of arrays
 - Linked structures require extra space for storing pointer fields
 - Linked lists do not allow efficient random access to items
 - Arrays allow better memory locality and cache performance than random pointer jumping
- Dynamic memory allocation provides us with flexibility on how and where to use limited storage resources

Comparison: Linked Lists vs. Arrays

- Both lists and arrays can be thought of a recursive objects:
 - Lists: chopping off the first element of a linked list leaves a smaller linked list
 - Lists are recursive objects
 - Splitting the first *k* elements off an n element array give two smaller arrays, of size *k* and *n-k*, respectively
 - Arrays are recursive objects
 - This shows us that lists are amenable to efficient (recursive) divide-and-conquer algorithms, such as binary search and quicksort