04-630

Data Structures and Algorithms for Engineers

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Lecture 5

Searching and Sorting Algorithms

- Linear Search & Binary Search
- In-place sorts
 - Bubble Sort
 - Selection Sort
 - Insertion Sort
- Not-in-place sort
 - Quicksort
 - Mergesort
- Characteristics of a good sort

Linear (Sequential) Search

Linear (Sequential) Search

- Begin at the beginning of the list
- Proceed through the list, sequentially and element by element,
- Until the key is encountered or Until the end of the list is reached

Linear (Sequential) Search

- Note: we treat a list as a general concept, decoupled from its implementation
- The order of complexity is O(n)
- The list does not have to be in sorted order

Implementation of linear search in C

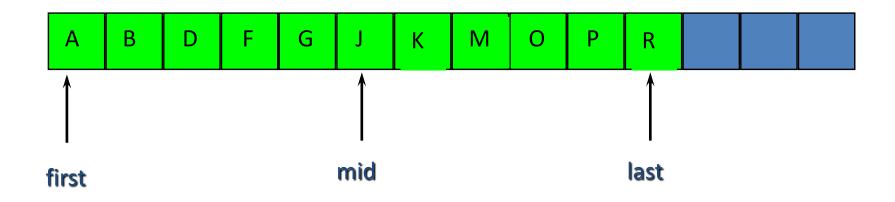
int linear_search(item_type s[], item_type key, int low, int high) {

```
int i;
 i = low;
 while ((s[i] != key) && (i < high)) {
     i = i+1;
 }
 if (s[i] == key) {
     return (i);
 }
 else {
     return(-1);
 }
```

}

- If the list is sorted, we can use a more efficient $O(\log_2(n))$ search strategy
- Check to see whether the key is
 - equal to
 - less than
 - greater than

the middle element



- If key is equal to the middle element, then terminate (found)
- If key is less than the middle element, then search the left half
- If key is greater than the middle element, then search the right half
- Continue until either
 - the key is found or
 - there are no more elements to search

Implementation of Binary_Search

Pseudo-code

binary_search(list, key, lower_bound, upper_bound)

identify sublist to be searched by setting bounds on search

REPEAT

get middle element of list
if middle element < key
then reset bounds to make the right sublist
the list to be searched
else reset bounds to make the left sublist
the list to be searched
UNTIL list is empty or key is found</pre>

Implementation of binary search in C (iterative approach)

```
typedef char item_type;
```

int binary_search(item_type s[], item_type key, int low, int high) {

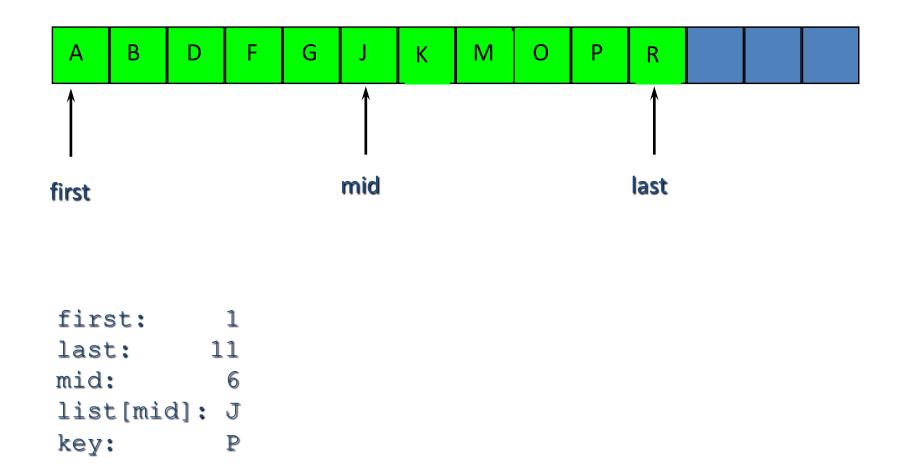
```
int first, last, mid;
first = low;
last = high;
do {
     mid = (first + last) / 2;
     if (s[mid] < key) {</pre>
         first = mid + 1;
     }
     else {
         last = mid -1;
     }
} while ( (first <= last) && (s[mid] != key) );</pre>
if (s[mid] == key)
     return (mid);
else
     return (-1);
```

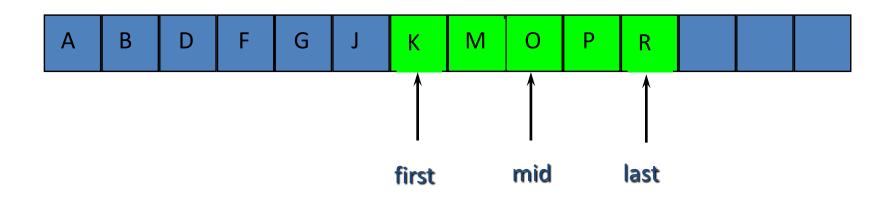
}



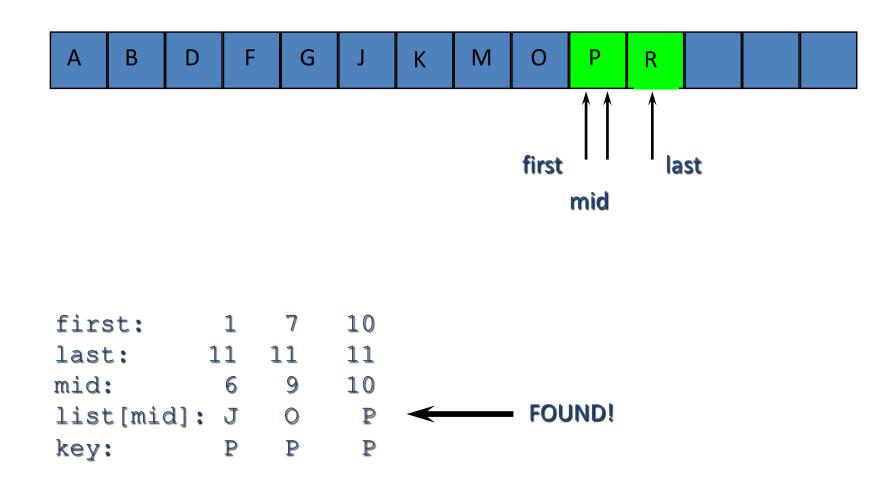
first:
last:
mid:
list[mid]:
key: P







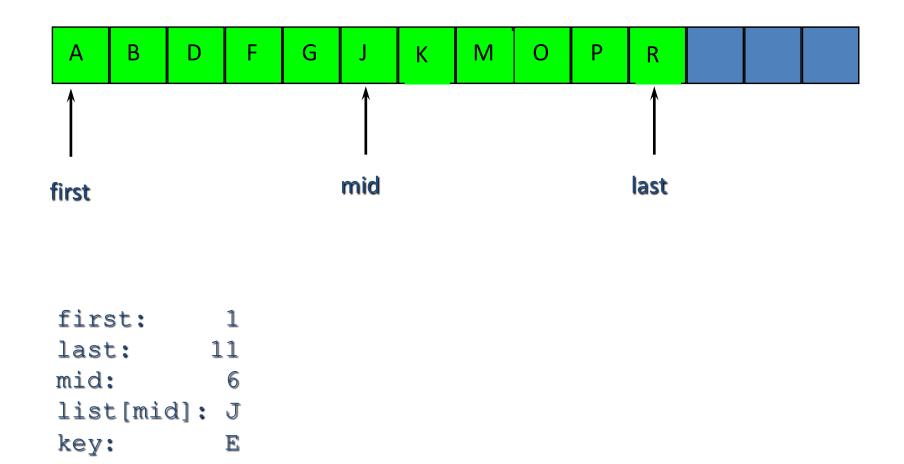
| first: | 1 | 7 |
|-----------|--------------|----|
| last: | 11 | 11 |
| mid: | 6 | 9 |
| list[mid] | : J | 0 |
| key: | \mathbb{P} | ₽ |

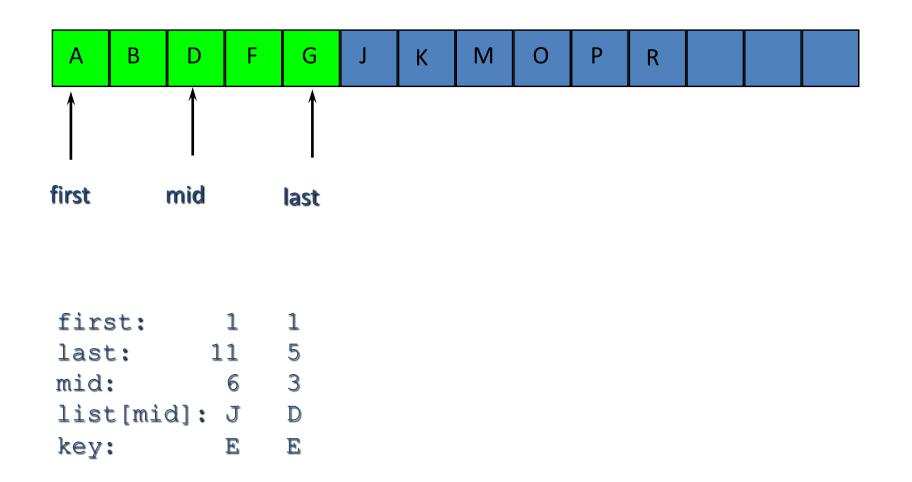


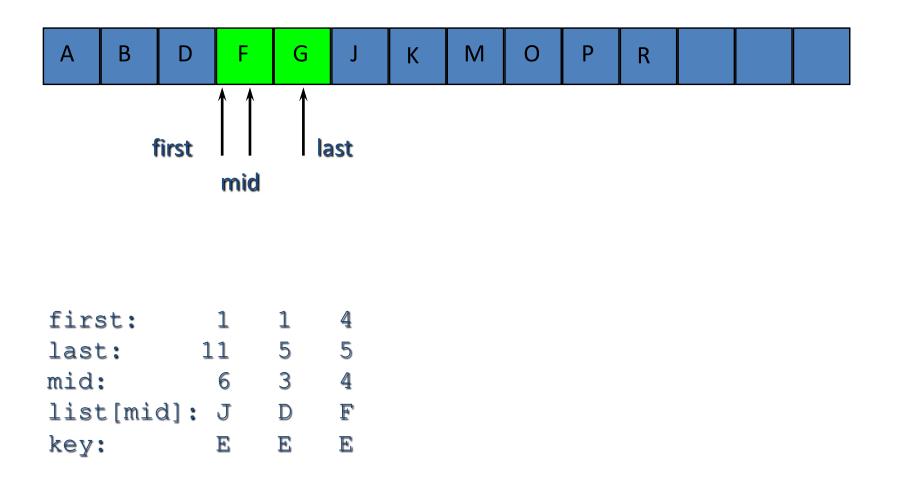


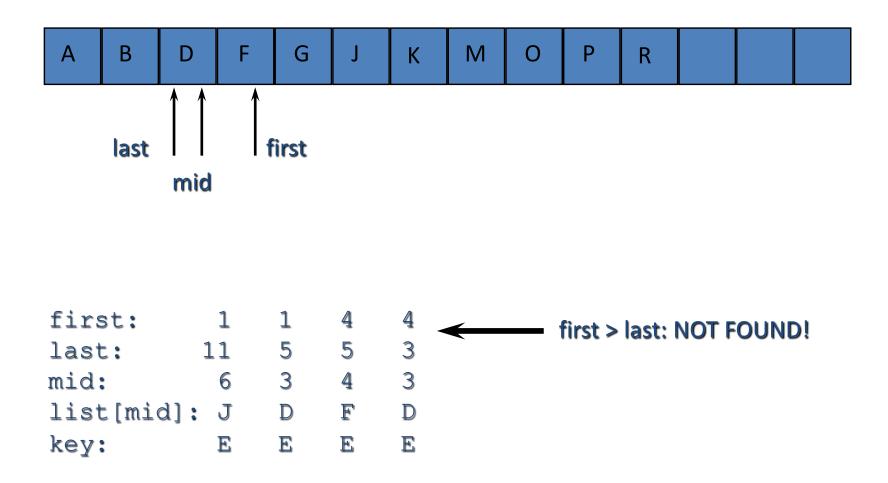
first:
last:
mid:
list[mid]:
key: E











Implementation of binary search in C (recursive approach)

```
typedef char item_type;
```

```
int binary_search(item_type s[], item_type key, int low, int high) {
```

```
int mid;
```

```
if (low > high) return (-1); /* key not found */
mid = (low + high) / 2;
if (s[mid] == key) return(mid);
if (s[mid] > key) {
   return(binary_search(s, key, low, mid-1));
}
else {
   return(binary_search(s, key, mid+1, high));
}
```

}

Sorting Algorithms

The Sorting Problem

Input: A sequence of *n* numbers $< a_1, a_2, \dots a_n >$

Output: the permutation (reordering) of the input sequence such that $a_1 \le a_2 \le ... \le a_n$

Sorting Algorithms

- In-place sorts
 - Small number of elements stored outside the input data structure
 - Additional space requirements O(1)
 - Tradeoff: more computationally-complex algorithms (slower sorts)
 - Bubble Sort
 - Selection Sort
 - Insertion Sort

Sorting Algorithms

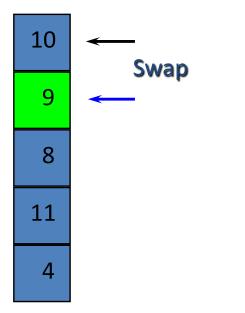
- Not-in-place sort
 - Additional space requirements not O(1)
 - Tradeoff: less computationally-complex algorithms but greater memory requirements (possibly unpredictable)
 - Quick Sort
 - Merge Sort
- Characteristics of a good sort

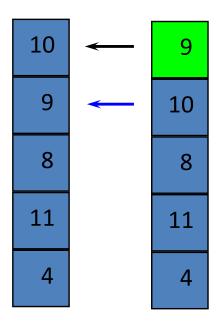
- Assume we are sorting a list represented by an array A of n integer elements
- Bubble sort algorithm in pseudo-code

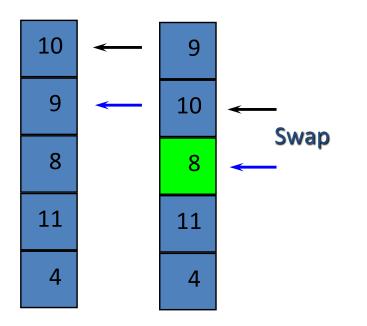
FOR every element in the list, proceeding from the first to the last

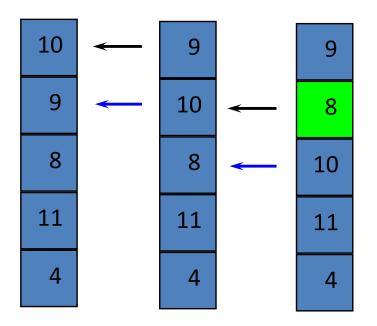
WHILE list element > previous list element bubble element back (up) the list by successive swapping with the element just above/prior it

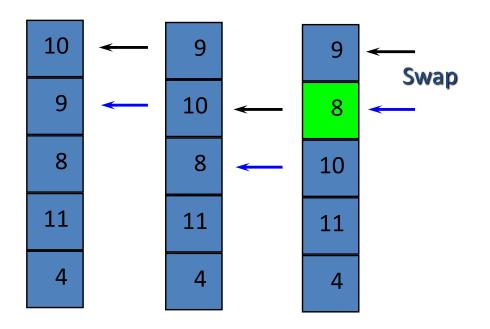
| | 10 | 9 | 8 | 11 | 4 | |
|--|----|---|---|----|---|--|
|--|----|---|---|----|---|--|

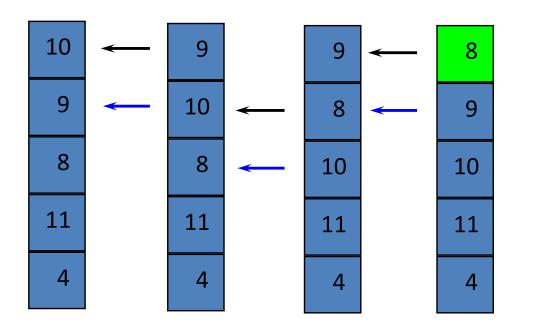


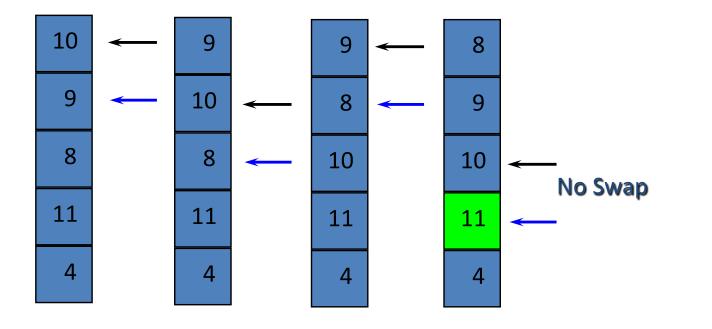


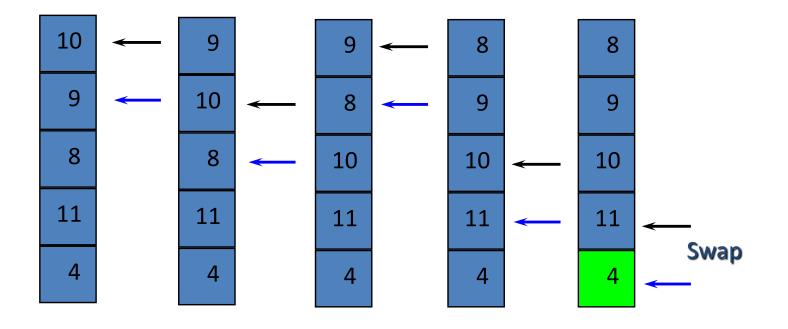


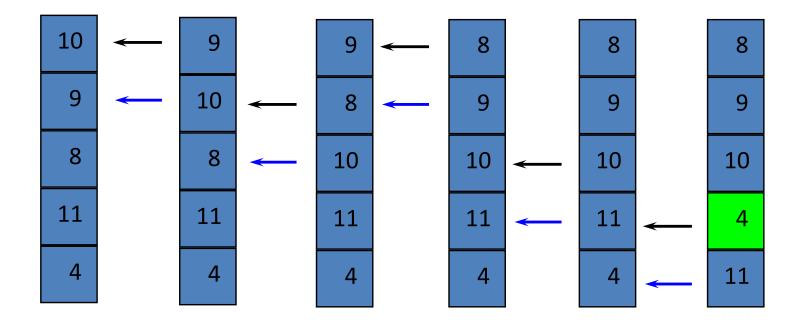


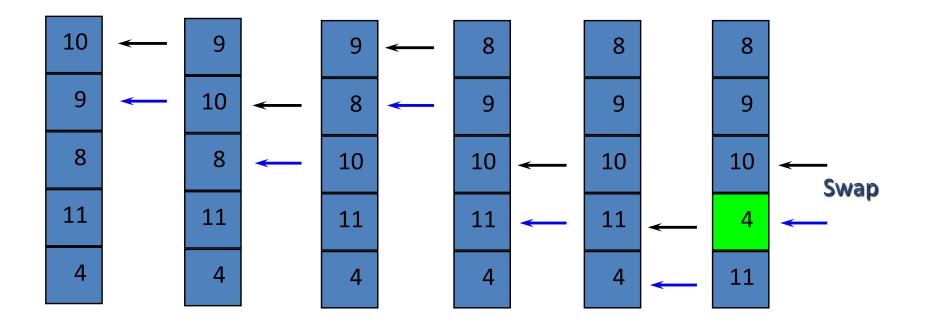


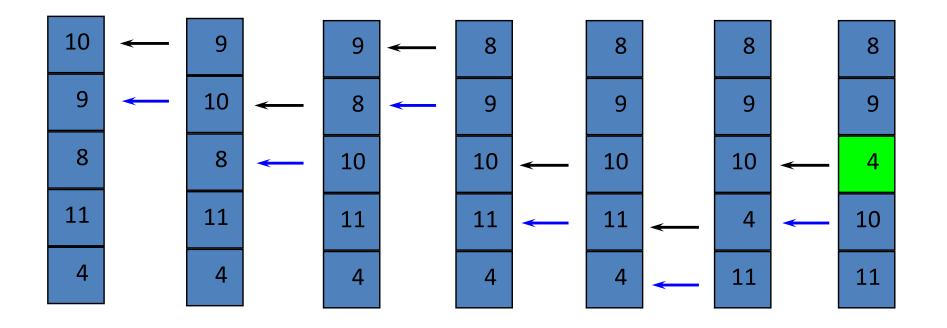


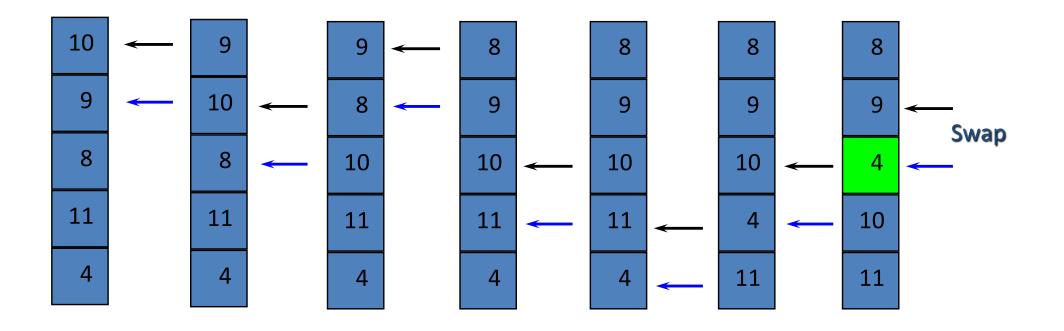


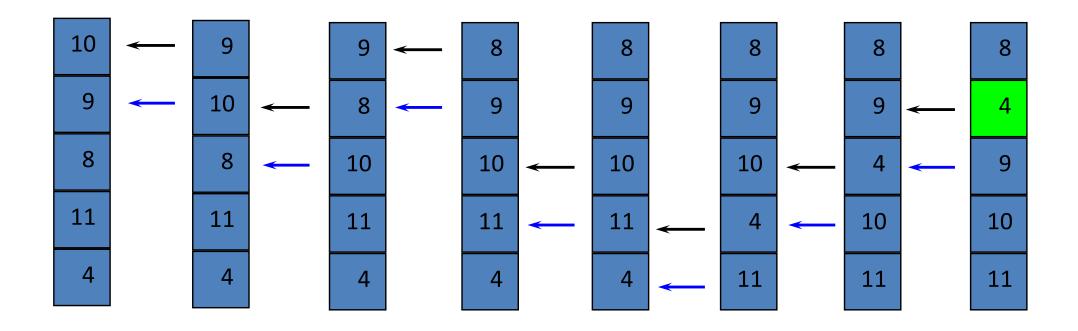


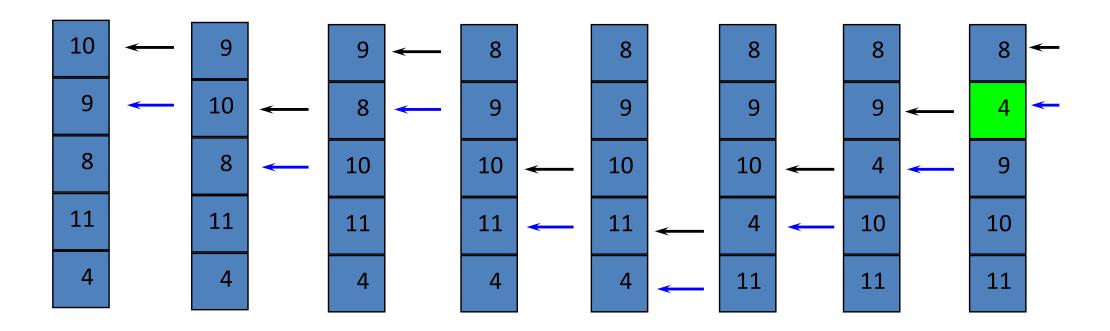






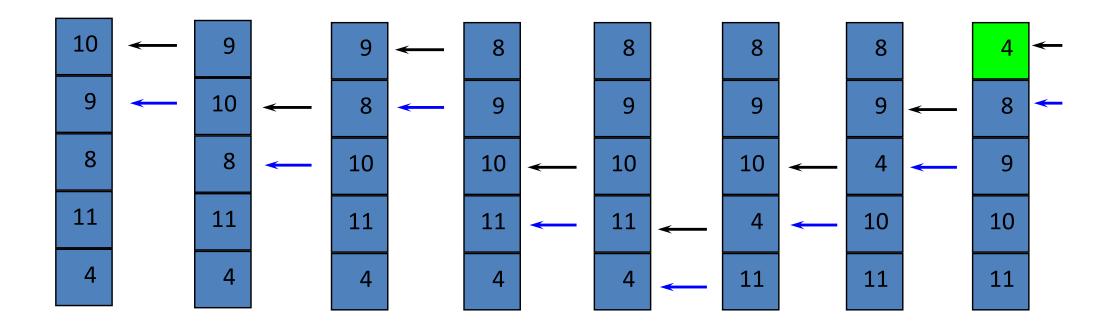






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Swap



Implementation of Bubble_Sort()

```
int bubble_sort(int *a, int size) { // int a[]
   int i,j, temp;
   for (i=0; i < size-1; i++) { // why?</pre>
      for (j=i; j >= 0; j--) {
         if (a[j] > a[j+1]) {
            /* swap */
            temp = a[j+1];
            a[j+1] = a[j];
            a[j] = temp;
         }
      }
   }
}
```

A few observations:

- we don't usually sort numbers; we usually sort records with keys
 - the key can be a number
 - or the key could be a string
 - the record would be represented with a **struct**
- The swap should be done with a function (so that a record can be swapped)
- We can make the preceding algorithm more efficient. How?
 (hint: do we always have to bubble back to the top?)

Exercise: implement these changes and write a driver program to test:

- the original bubble sort
- the more efficient bubble sort
- the bubble sort with a swap function
- the bubble sort with structures
- compute the order of time complexity of the bubble sort

Selection Sort

Example:

- Shaded elements are selected
- Boldface elements are in order

| Initial Array | 29 | 10 | 14 | 37 | 13 |
|----------------------------|----|----|----|----|----|
| After 1 st swap | 29 | 10 | 14 | 13 | 37 |
| After 2 nd swap | 13 | 10 | 14 | 29 | 37 |
| After 3 rd swap | 13 | 10 | 14 | 29 | 37 |
| After 4 th swap | 10 | 13 | 14 | 29 | 37 |

Selection Sort

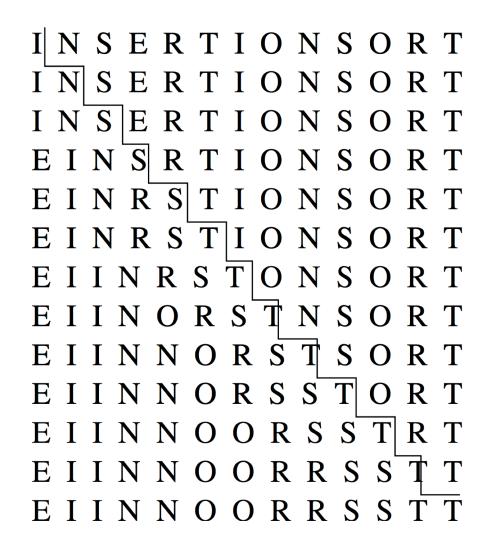
- Assume we are sorting a list represented by an array A of n integer elements
- Selection sort algorithm in pseudo-code

```
last = n-1
Do
    Select largest element from a[0..last]
    Swap it with a[last]
    last = last-1
While (last >= 1)
```

Selection Sort

```
typedef int DataType;
void selectionSort(DataType a[], int n) {
   DataType temp;
   int index of largest, index, last;
   for(last= n-1; last >= 1; last--) {
       // select largest item in a[0..last]
       index of largest = 0;
       for(index=1; index <= last; index++) {</pre>
          if (a[index] > a[index of largest])
            index of largest = index;
      }
      // swap largest item with last element
      temp = a[index of largest];
       a[index of largest] = a[last]);
       a[last]) = temp;
   }
}
```

Insertion Sort



Insertion Sort

```
typedef int DataType;
insertion_sort(DataType a[], int n) {
   int i,j;
   int temp;
   for (i=1; i<n; i++) {</pre>
      j=i;
      while ((j>0) && (a[j] < a[j-1])) {</pre>
         temp = a[j-1]; // swap
         a[j-1] = a[j];
         a[j] = temp;
         j = j-1;
      }
   }
}
```

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