

Introduction to Cognitive Robotics

Module 3: Mobile Robots

Lecture 3: Relative position estimation using inertial sensors

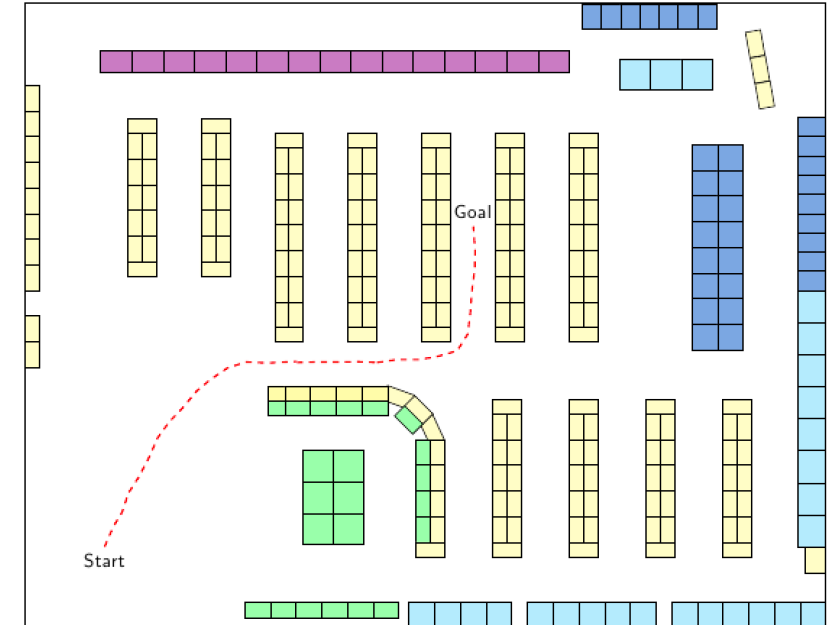
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Carnegie Mellon University Africa

www.vernon.eu

Localization: The Position Estimation Problem

Two approaches

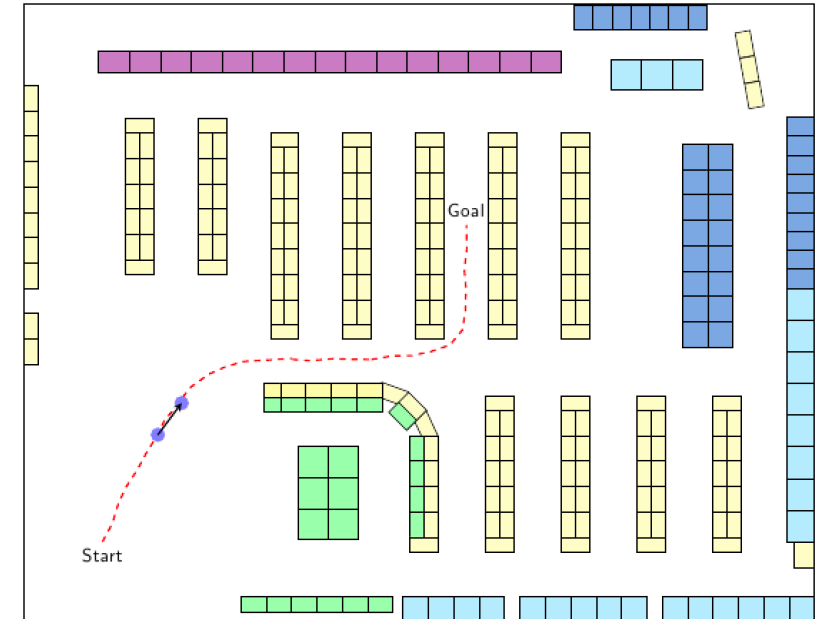
1. Absolute position estimation
2. **Relative** position estimation



Relative Position Estimation

Detect the change in the position and orientation of the robot: $(\Delta x, \Delta y, \Delta \theta)$

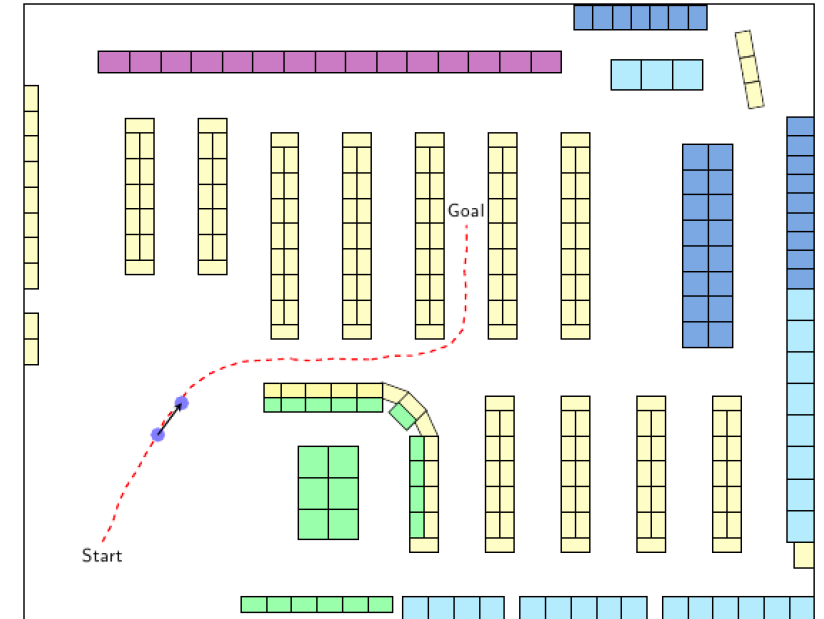
Combine the previous estimate and the change to determine the new estimate of the robot position



Relative Position Estimation

Options for detecting change in relative position:

- Inertial sensors
- Odometry



Inertial Position Estimation

Options for detecting change in relative position:

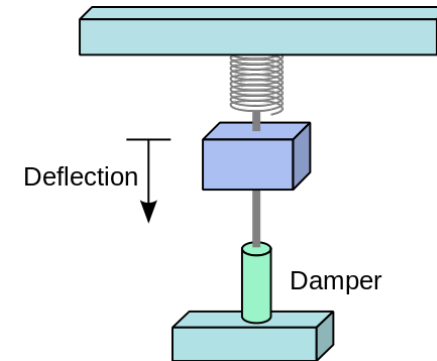
- Inertial sensors
 - Accelerometers sense change in position
 - Gyroscopes sense change in orientation

Inertial Position Estimation

Option for detecting change in relative position:

Accelerometer

- Acceleration causes a deflection of a mass
- An open-loop accelerometer senses the deflection of the mass
 - Acceleration is determined from the displacement, mass, and spring constant
- A closed-loop accelerometer counteracts the force on the mass, canceling the motion
 - Acceleration is determined from the counteracting force



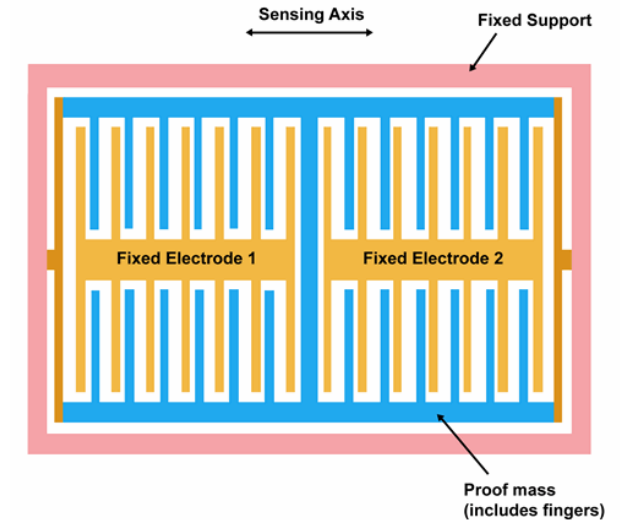
Source: https://en.wikipedia.org/wiki/Inertial_navigation_system

Inertial Position Estimation

Option for detecting change in relative position:

Accelerometer

- Miniature microelectromechanical systems (MEMS) accelerometer
- When the sensor is subjected to a linear acceleration along its sensing axis
 - The proof mass and its fingers become displaced with respect to the fixed electrode fingers
 - The differential capacitance between the moving and fixed silicon fingers is measured
 - This is proportional to the acceleration



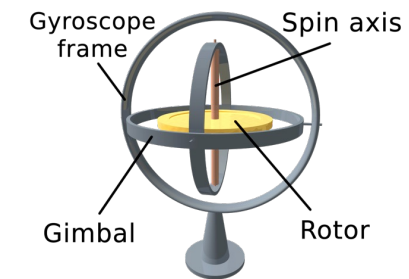
Source: <https://www.siliconsensing.com/technology/mems-accelerometers/>

Inertial Position Estimation

Option for detecting change in relative **orientation**:

Gyroscope

- A gyroscope is used for measuring or maintaining orientation and angular velocity
- Rate gyros measure angular **rate of change** of rotation
 - Change in orientation is computed by integration



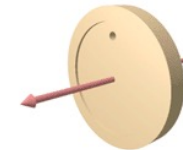
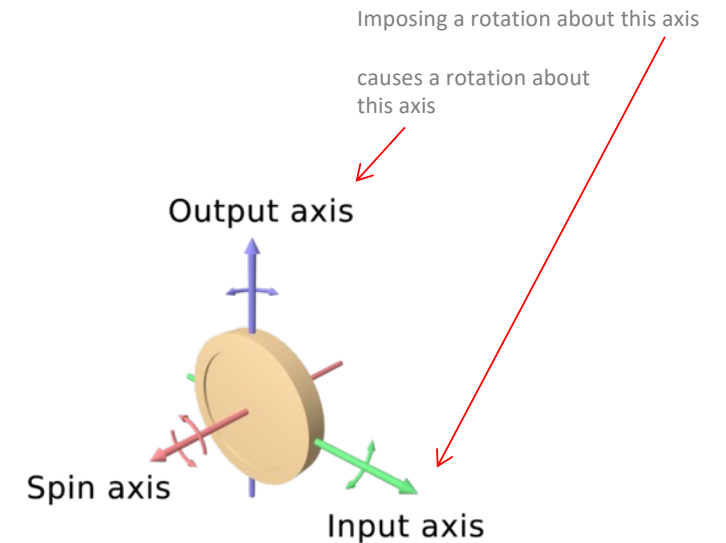
Source: <https://en.wikipedia.org/wiki/Gyroscope>

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Source: <https://en.wikipedia.org/wiki/Gyroscope>

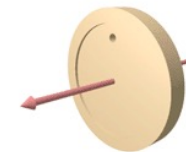
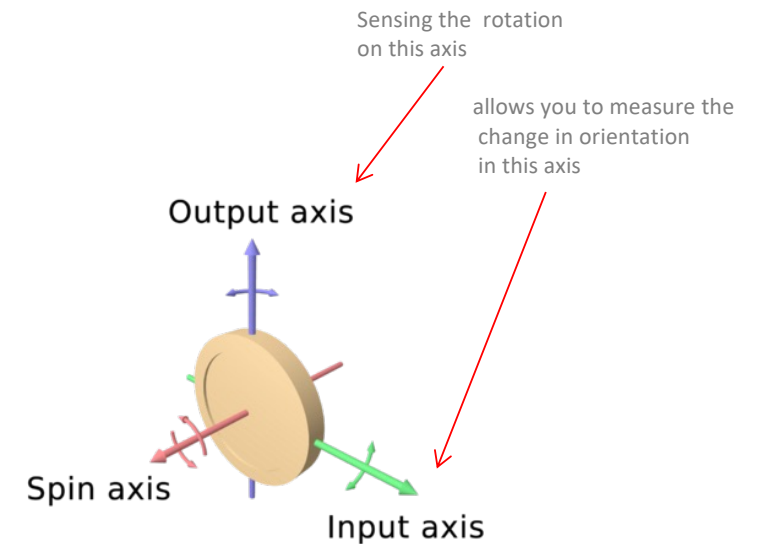
See <https://www.youtube.com/watch?v=mRZGdvJQnPU> for an explanation of gyroscopic precession, i.e., the relationship between angular momentum and applied torque

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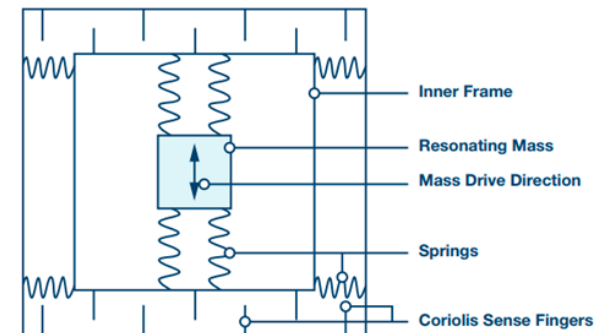
Source: <https://en.wikipedia.org/wiki/Gyroscope>

Inertial Position Estimation

Option for detecting change in relative **orientation**:

Gyroscope

- Miniature microelectromechanical systems (MEMS) gyroscope
- One approach is to use a vibrating mass and the resultant displacement in an orthogonal direction to sense the rotation



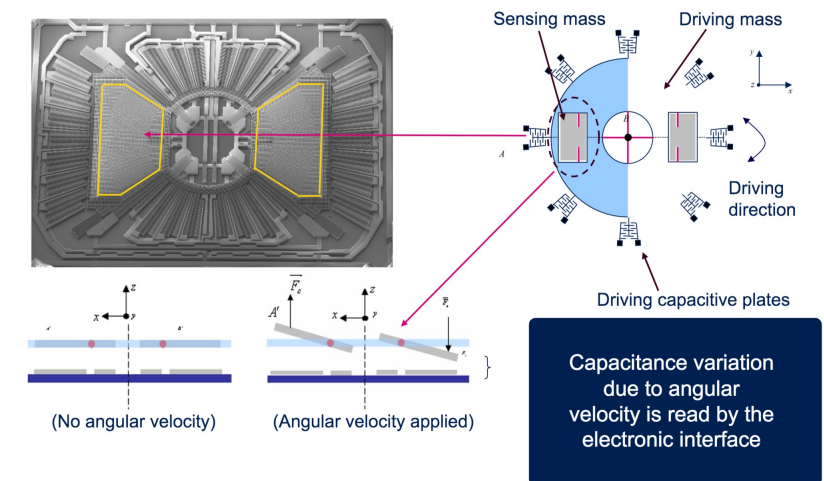
Source: <https://www.analog.com/en/technical-articles/mems-gyroscope-provides-precision-inertial-sensing>

Inertial Position Estimation

Option for detecting change in relative **orientation**:

Gyroscope

- Miniature microelectromechanical systems (MEMS) gyroscope
- Others use capacitive sensing of a displaced mass to measure the rotation (angular velocity)

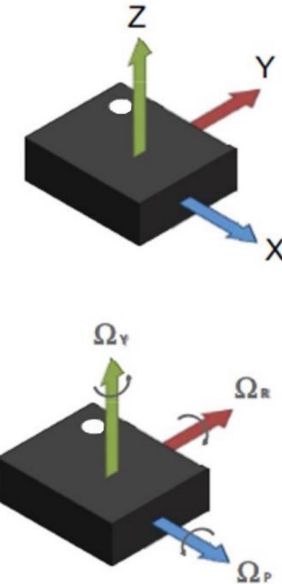


Source: <https://www.st.com/en/mems-and-sensors/gyroscopes.html>

Inertial Position Estimation

Inertial Measurement Unit IMU

- Combines **three** accelerometers and **three** gyroscopes
- In three orthogonal (x, y, z) directions
- To sense change in position and orientation



Source: <https://www.st.com/resource/en/datasheet/asm330lhh.pdf>

Inertial Position Estimation

Options for detecting change in relative position:

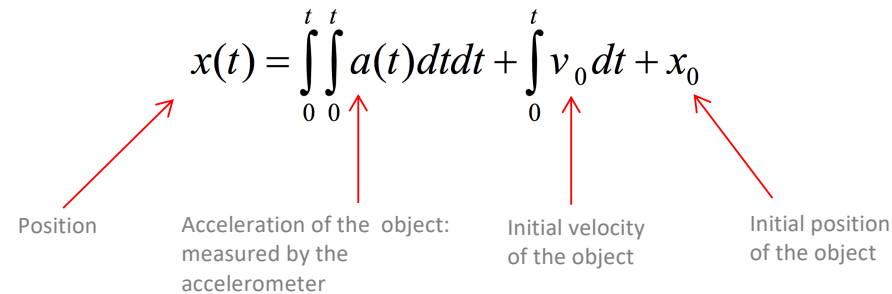
– So far

- **Accelerometers** sense acceleration ... we want **change in position**
- **Gyroscopes** sense rate of change of orientation ... we want **orientation**
- We get what we want by **integrating** the sensed data with respect to time

Inertial Position Estimation

Double integration of acceleration to determine position

Ideally, the position x of a body at any time t can be determined from the time-dependent acceleration of that body

$$x(t) = \int_0^t \int_0^t a(t) dt dt + \int_0^t v_0 dt + x_0$$


The diagram illustrates the equation for position estimation. Red arrows point from descriptive text labels below to specific parts of the equation: one arrow points from 'Position' to $x(t)$; another points from 'Acceleration of the object: measured by the accelerometer' to the inner integral $\int_0^t a(t) dt$; a third points from 'Initial velocity of the object' to v_0 ; and a fourth points from 'Initial position of the object' to x_0 .

Position

Acceleration of the object:
measured by the
accelerometer

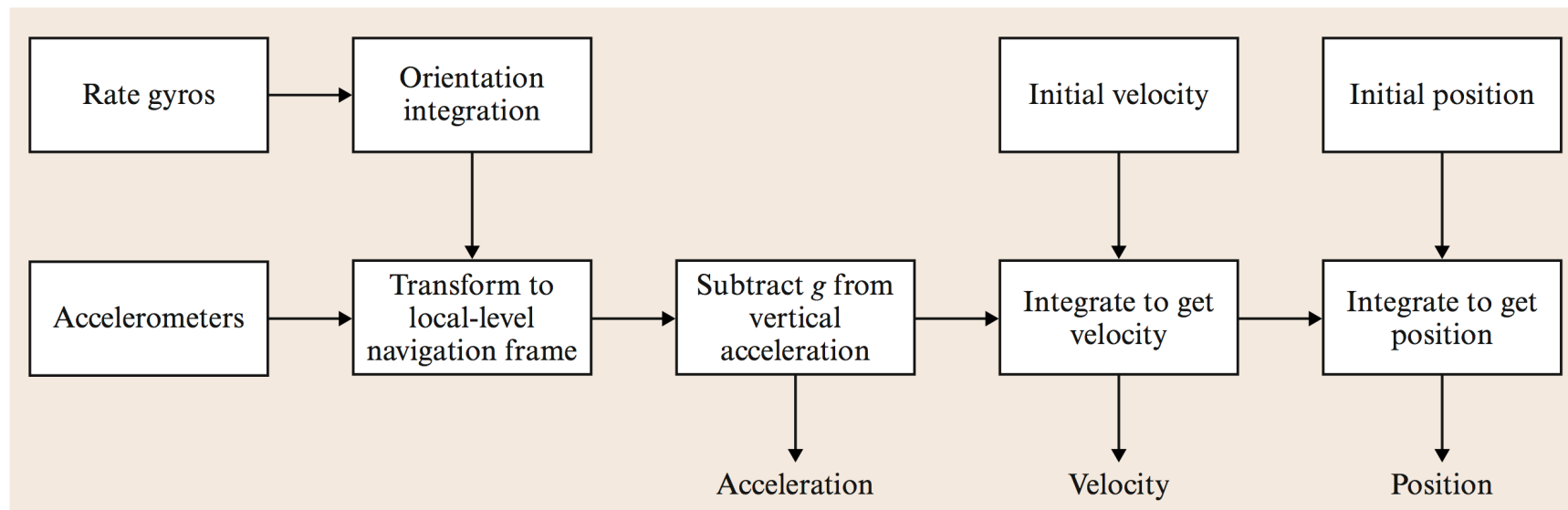
Initial velocity
of the object

Initial position
of the object

Source: <https://d10bqar0tuhard.cloudfront.net/en/document/AN013-Position-determination-using-Accelerometers.pdf>

Inertial Position Estimation

Block diagram for estimating position with an IMU



Source: B. Siciliano and O. Khatib (eds.), Springer Handbook of Robotics, Springer, 2008.

Inertial Position Estimation

- Precise estimate if
 - initial estimate of v_0 and s_0 are precise
 - measurement of $a(t)$ is precise

For more information on how to minimize errors with a MEMS accelerometer, see the technical note here:
<https://d10bqar0tuhard.cloudfront.net/en/document/AN013-Position-determination-using-Accelerometers.pdf>

- However, sensors are not perfect, and errors arise
- Errors accumulate without bounds
 - Double integration means that the errors grow quadratically
 - Need to reset the position from time to time, e.g., using absolute position estimation

Reading

M. Mataric, The Robotics Primer, MIT Press, 2007. Chapter 7.